



# Radar Recognition of Multi-Propeller Drones using Micro-Doppler Line Spectra

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# Outline

- Introduction
- Simulation model for drone micro-Doppler spectrum
- Drone micro-Doppler features analysis and selection
- Application of features to simulated data
- Conclusion

# Introduction

- Drones are popular
  - Environmental monitoring, delivery, emergency services



Drone revealing fire damage to Notre Dame

- They pose threats
  - Collision hazards, privacy violation, illegal reconnaissance, smuggling, terrorism

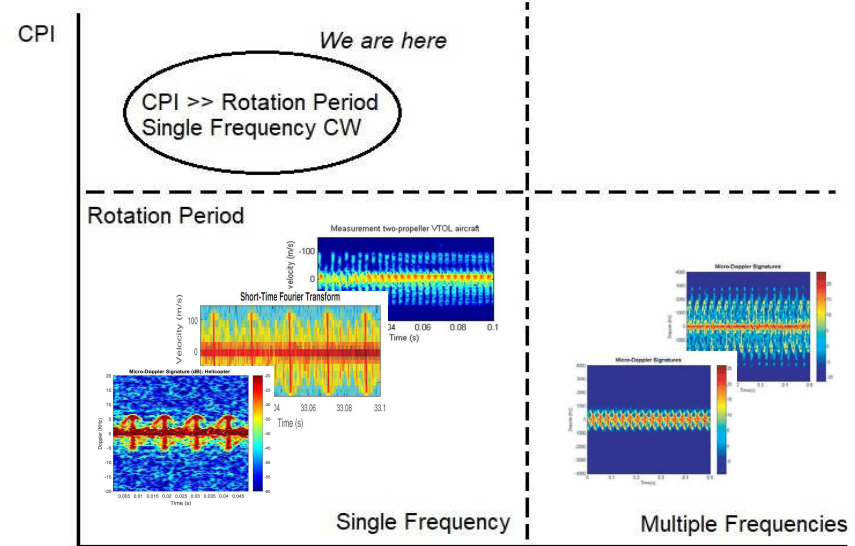
# Introduction

- Response to these threats
  - Detection, Tracking, Characterization, Classification
  - then – acting (interception / destruction / jamming)
- All these tasks can be done based on **radar micro-Doppler patterns**
  - Long range sensing, stable in most weather and light conditions, provides range and velocity information
- What do we need to know for about drones?
  - It is necessary to understand the relations between the observed micro-Doppler pattern, radar parameters and properties of specific drone's rotating parts:
  - Algorithms for aforementioned sensing tasks...

# Objectives of the study

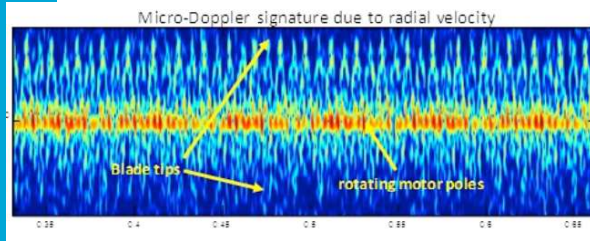
To study the drone's micro-Doppler pattern that are observed by a radar and to select the features that are most informative/useful for drone's type identification/recognition

- Use previously developed and presented general approach for drone's simulation and simplified EM model of scattered on drone signal
- Concentrate on the case of long Coherent Processing Interval (CPI)

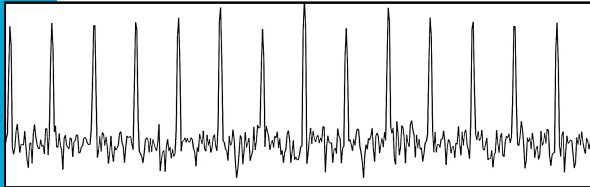


# Short and Long Coherent Processing Intervals

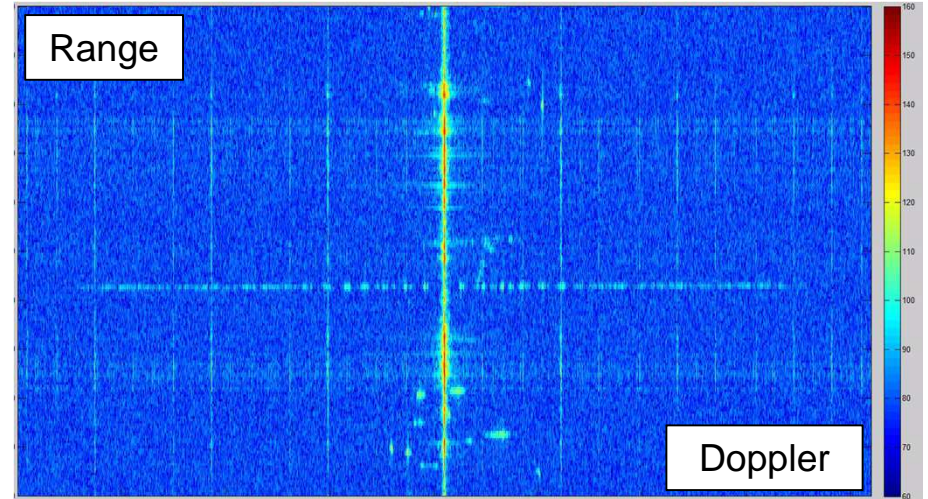
Short CPI  $\ll$  Rotation Period



Long CPI  $\sim$  Rotation Period



Line spectrum



DJI Matrix-600, PARSAX radar, HH polarisation,  
Range 9 km, 3.315 GHz, PRI = 240 $\mu$ s, B=16.8MHz,  
PRF = 4.17 kHz, CPI = 0.98 s, SNR  $\sim$  20 dB

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# Our proposed simulation approach

## Models

Precise EM  
(FEKO)

Simple  
(thin-wires)

## Measurements

Anechoic  
Chamber

Angular  
dependence of  
blade/propeller  
scattering  
coefficient

## One rotor/propeller

Rotation  
Frequency

Radar:  
PRF, CPI

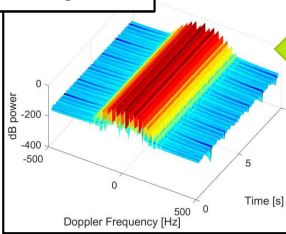
Time  
dependence

Sampling

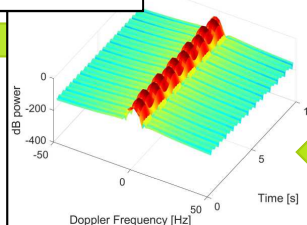
Drone's  
Geometry,  
LOS  
Orientation

Coherent  
Sum  
at Drone's  
Phase  
Center

Long CPI



Short CPI

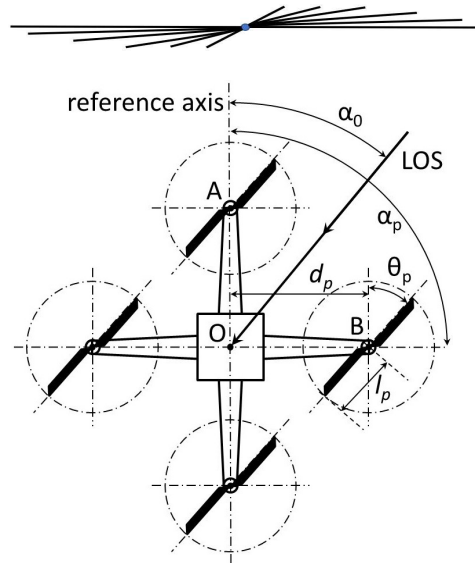


Doppler FFT as  
Function of Time



# Simulation model for drone micro-Doppler spectrum

- Simulation model of drone's EM reflection (HH)



Thin-wire model of multi-propeller drone and each single propeller

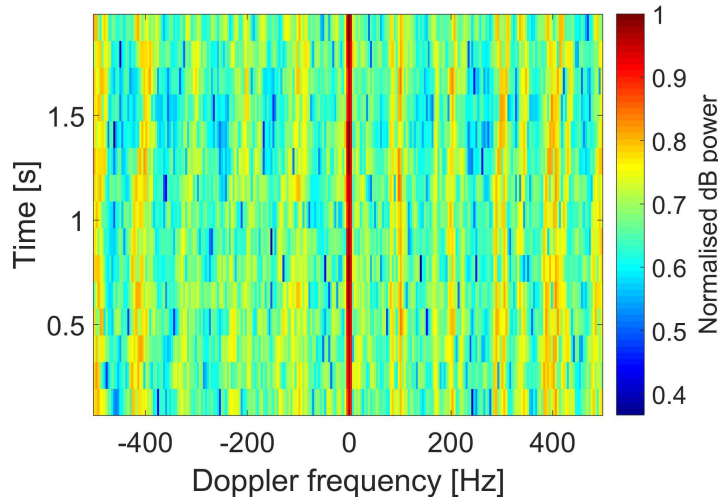
$$\begin{aligned}
 E^{drone}(t, r_0) &\sim \sum_{p=1}^P E_p^{prop}(t, r_p, \theta_{p,b,w}, l_{p,b,w}) \\
 &= \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W E_{p,b,w}^{wire}(t, r_p, \theta_{p,b,w}, l_{p,b,w}) \\
 &= \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W \int_0^{l_{p,b,w}} j\eta \frac{ke^{-jkr_p}}{4\pi r_p} \\
 &\quad \times E_{r_0}^{in}(t) \sin^2(\theta_{p,b,w} + \Omega_p t) \\
 &\quad \times e^{j2ky'_{p,b,w} \cos(\theta_{p,b,w} + \Omega_p t)} dy'_{p,b,w} \\
 &= \sum_{p=1}^P j\eta \frac{ke^{-jkr_p}}{4\pi r_p} \cdot E^{propeller}
 \end{aligned}$$

where  $r_p = r_0 - d_p \cdot \cos(\alpha_p - \alpha_0)$ .

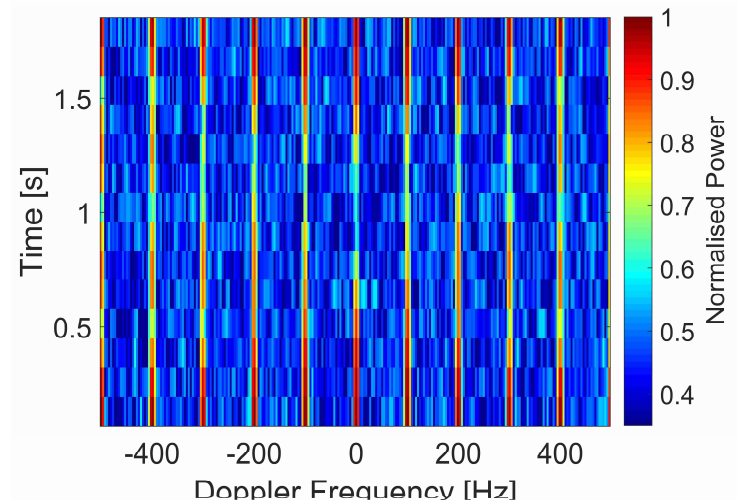
\* Synthesis and synchronisation of propellers

# Simulation model for drone micro-Doppler spectrum

- Drone micro-Doppler pattern from simulation model
  - Doppler processing to EM reflection signal
  - Linear pattern in long CPI circumstance: S-band, DJI M600 drone, radar CPI much longer than propeller rotation period



Micro-Doppler pattern of hexa-copter  
(PARSAX radar measurement)



Micro-Doppler pattern of hexa-copter  
(Thin-wire model simulation)

# Simulation model for drone micro-Doppler spectrum

- Thin-wire model proposed for the simulation of drone micro-Doppler spectrum
  - Validated in S-band
  - Taking radar setup parameters and drone's properties as input variables
  - Generating line spectral micro-Doppler pattern within long CPI circumstance

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# Drone micro-Doppler features analysis

- Simulation model rewritten in Bessel functions

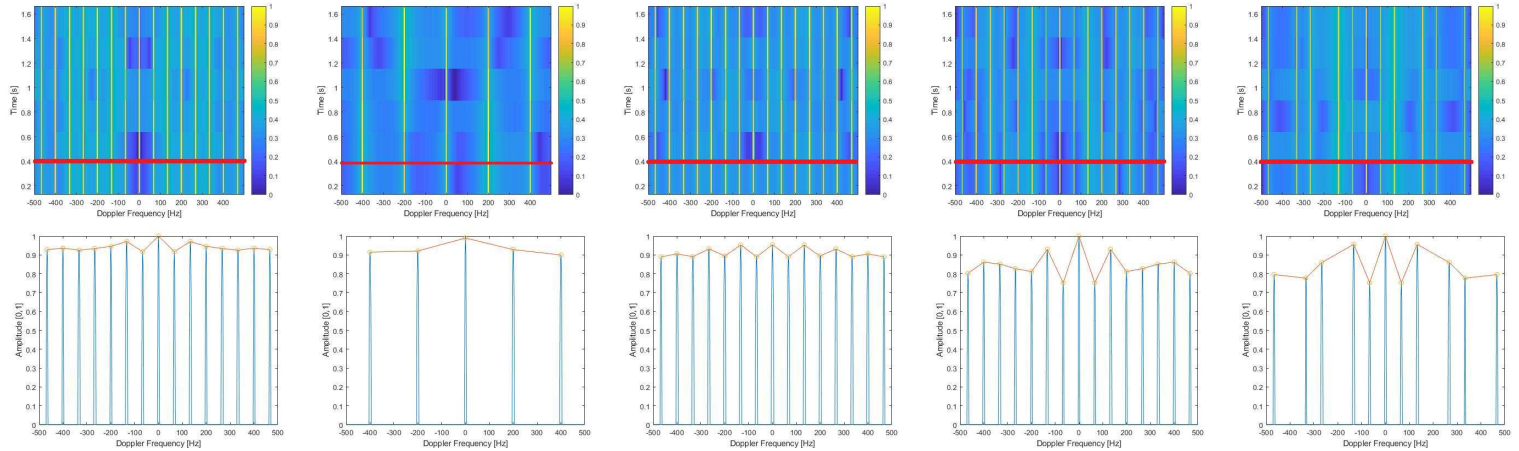
$$E^{drone}[n] \sim \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W s_{p,b,w}^{wire}[n] \quad \left. \vphantom{\sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W} \right\} \text{Sums over wires, blades, propellers}$$

$$= \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W \underbrace{\frac{\eta e^{-j\frac{2\pi}{\lambda} r_p}}{8\pi r_p}}_{\text{Drone geometry (extra phase, extra amplitude)}} \cdot \underbrace{\frac{\sin^2(\theta_{p,b,w} + \Omega_p t_s n)}{\cos(\theta_{p,b,w} + \Omega_p t_s n)}}_{\text{Propeller rotation period (extra amplitude)}} \cdot \left( \sum_{q=-\infty}^{\infty} \underbrace{e^{j\frac{\pi q}{2}}}_{\text{Bessel functions (amplitude)}} \underbrace{J_q\left(2\frac{2\pi}{\lambda} l_{p,b,w}\right) e^{j(\theta_{p,b,w} + \Omega_p t_s n)q}}_{\text{Harmonic components (frequency)}} - 1 \right)$$

- Influence factors: PRF, carrier frequency, drone's geometry, propeller's radius and rotation period
- Influence on the micro-Doppler spectrum: **Amplitude** and **frequency gap** of harmonic components

# Micro-Doppler pattern vs Drone's Properties

- Influence of drones' properties on spectral lines' amplitudes, locations, the total bandwidth of non-folded Doppler spectra



(a)

2 blades  
Short blades  
4 propellers  
No angle shift

(b)

3 blades  
Short blades  
4 propellers  
No angle shift

(c)

2 blades  
Long blades  
4 propellers  
No angle shift

(d)

2 blades  
Short blades  
4 propellers  
Random shift of initial angles

(e)

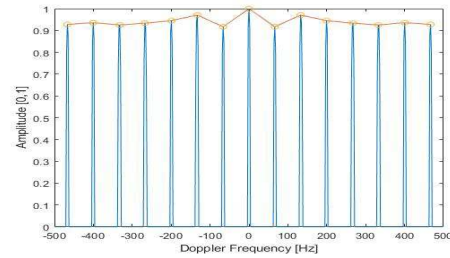
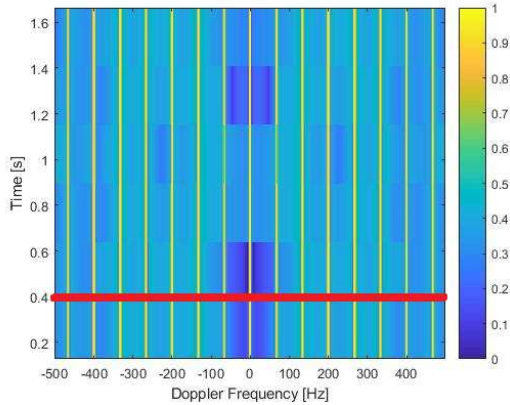
2 blades  
Short blades  
6 propellers  
No angle shift

Micro-Doppler patterns of drones and their cuts at some time moment 14

# Micro-Doppler pattern vs Propellers Velocities

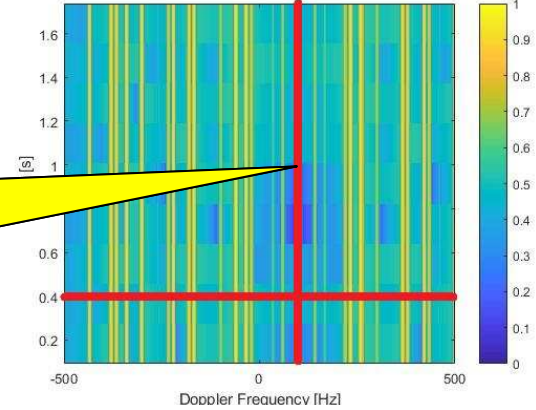
## Hovering

(propellers rotation is synchronous)

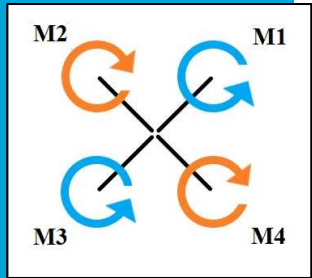
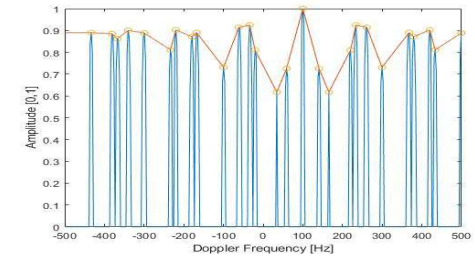
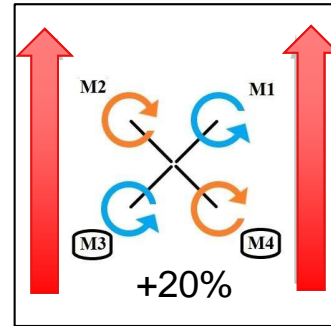


## Maneuvering

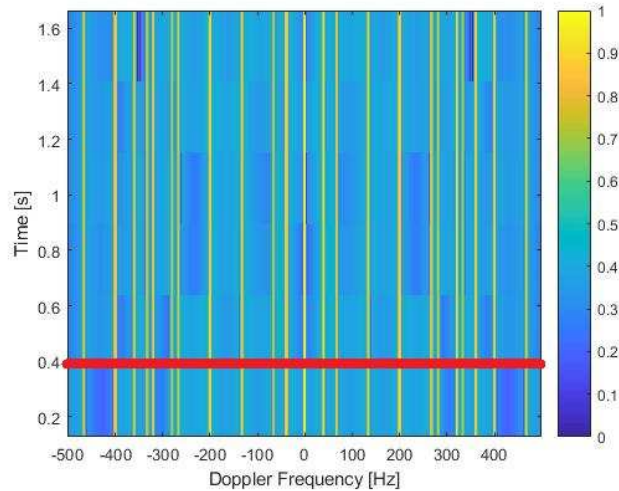
(propellers rotate with different velocities)



Patterns centres shift away from zero Doppler frequency



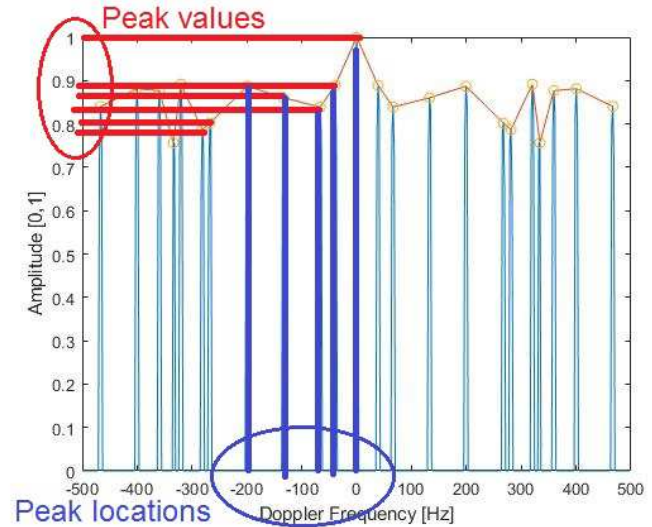
# Features for drones recognitions



An example of micro-Doppler pattern

**Location** = [0,0,1,0,0,...]

**Amplitudes** = [0.84,0.89,0.88,...,1,...]



Characteristics of line spectrum

[  $1 \times N_{CPI}$  ] vector, "1" if a peak appears

[  $1 \times N_{peaks}$  ] vector, peak values

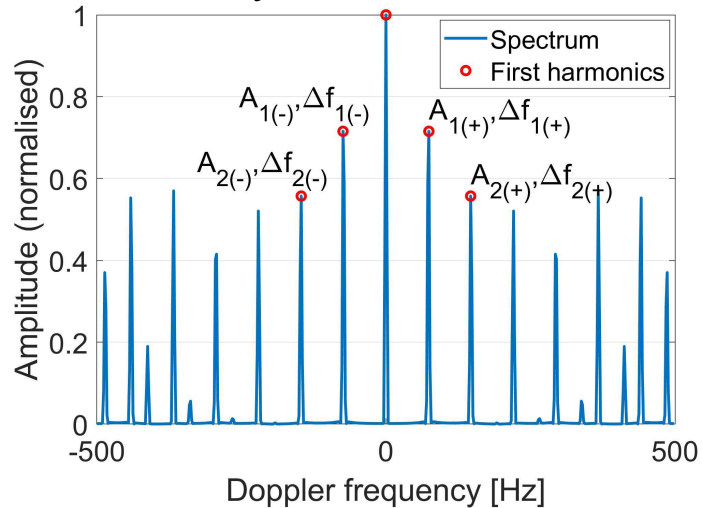
**Mean** (Amplitudes), **Standard Deviation** (Amplitudes), **Entropy** (Amplitudes)

**Features** = [ Location, Mean, Standard Deviation, Entropy ]

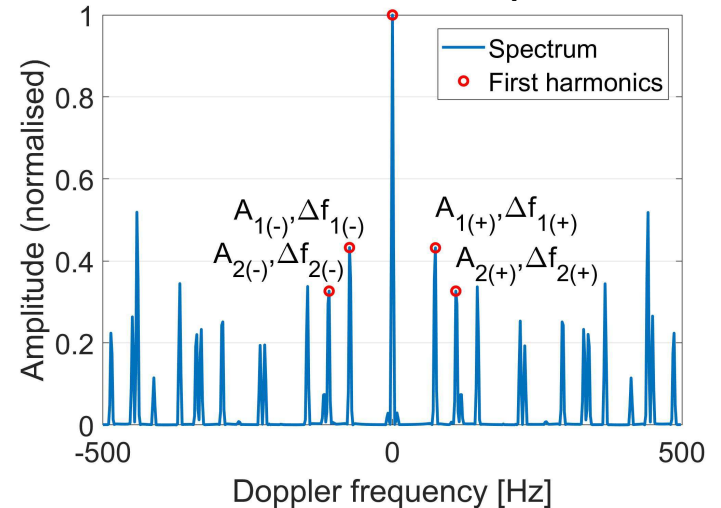


# Drone micro-Doppler features selection

- Features that characterize the micro-Doppler spectrum
  - **Amplitudes** and **frequencies** of harmonic components
  - Only first 4 harmonic components shown in this example



Micro-Doppler spectrum of hovering quad-copter



Micro-Doppler spectrum of maneuvering quad-copter

\* 2 amplitude modulation,  
\*\* Non-uniform frequency gap

# Drone micro-Doppler features selection


- Features selection for drone micro-Doppler spectrum in long CPI circumstance
  - Influential factors:
    - radar setup parameters
    - drone properties
  - Proposed features to characterize the spectrum:
    - Set of linear harmonics' amplitudes
    - Set of frequency gaps between them
    - Sub-sets
    - Their statistical moments

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# Application of features to simulated data

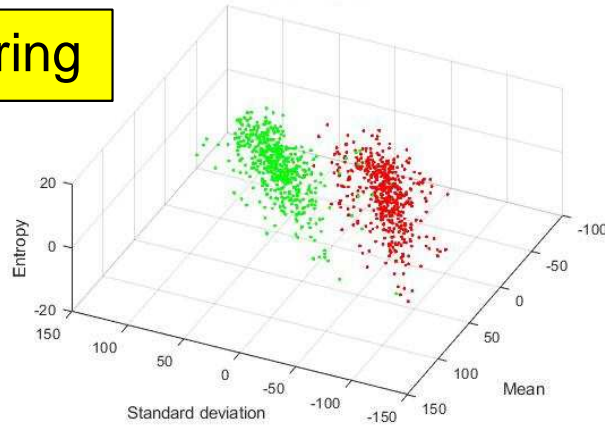
- Simulation data sets
  - Drones: Quad-, hexa-, octo-copter
  - Flight motion modes: Hovering, maneuvering

Combination of Input Variables	Drones & Flight Attitudes	Blade Length $l$ [m]	Arm Length $d_p$ [m]	Propeller Angular Velocity $\Omega$ [rpm]
	quadcopter hover	0.114	0.175	$2200 * [1, -1, 1, -1]$
	quadcopter cross range			$2200 * [1, -v_{asyn}, v_{asyn}, -1]$ $v_{asyn} = 1.5$
	hexacopter hover	0.267	0.567	$1800 * [1, -1, 1, -1]$
	hexacopter cross range			$1800 * [1, -v_{asyn}, v_{asyn}, -1]$ $v_{asyn} = 1.5$
	octocopter hover	0.267	0.567	$1500 * [1, -1, 1, -1]$
	octocopter cross range			$1500 * [1, -v_{asyn}, v_{asyn}, -1]$ $v_{asyn} = 1.5$

# Two classes recognition

Hovering

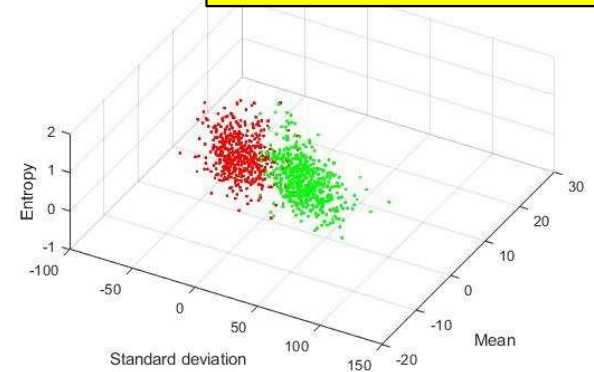
3D – only amplitudes' features



4-copter Truth 6-copter  
464 obs. 520 obs.

Decision	4-copter	462 observations (99.57%)	6 observations (1.15%)
	6-copter	2 observations (0.43%)	514 observations (98.85%)

Maneuvering



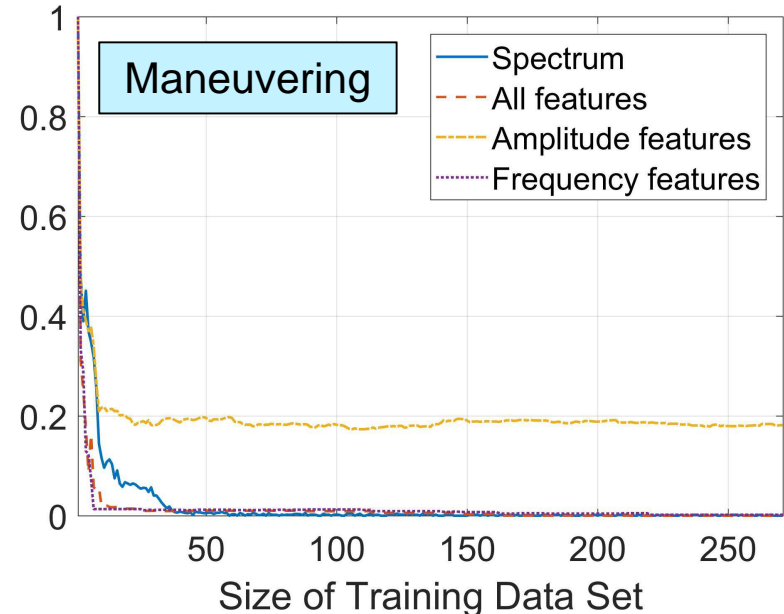
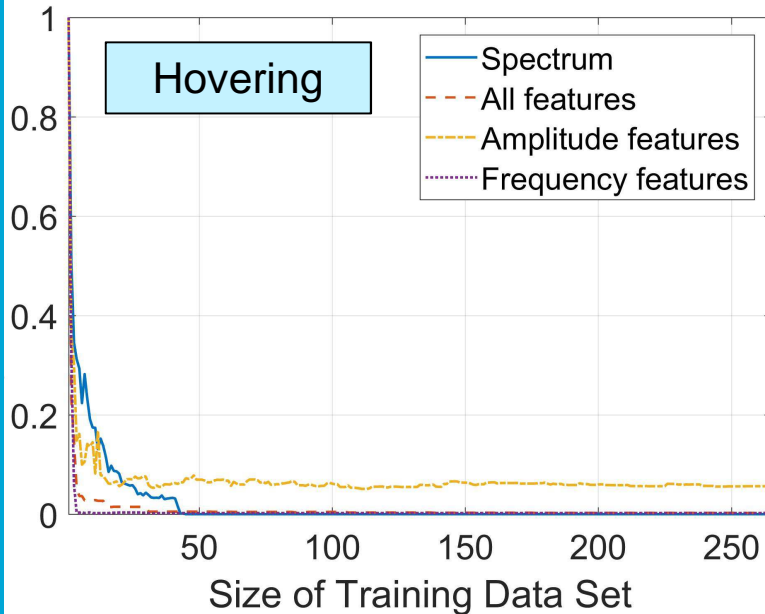
4-copter Truth 6-copter  
488 obs. 486 obs.

Decision	4-copter	454 observations (93.03%)	33 observations (6.79%)
	6-copter	34 observations (6.97%)	453 observations (93.2%)

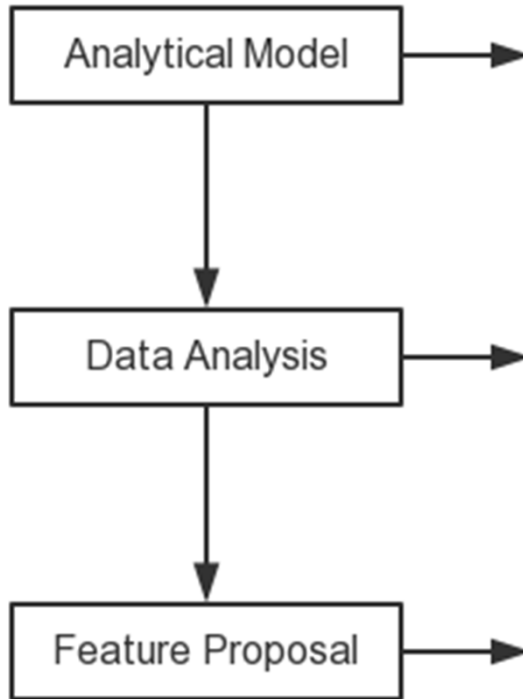
# Application of features to simulated data

- Classification results on simulated m-D data
  - SVM classifier, 5-fold cross validation
  - Amplitude and frequency gap of first 4 harmonic components

Probability of classification error



# Conclusion



- The simple model efficiently generates micro-Doppler patterns for any selected propeller, drone and radar setup parameters
- The parameters of micro-Doppler pattern are strongly influenced with propeller, drone and radar setup parameters
- The measured during long CPI line spectral micro-Doppler patterns of different drones are precisely characterized with set (and sub-sets) of peaks' amplitudes and frequencies

# *Questions?*